

The (a, b) – Status Indices of Central Graphs of Some Standard Graph

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Abstract: The sum of shortest distance between a vertex u from all other vertices of a graph G is called the index of the vertex u and is denoted by $\sigma(u)$. In this article, we have obtained, the (a, b) – status index [3] of central graphs of some standard graphs namely star graph, complete graph, cycle graph, wheel graph and friendship graph. Using this new index, we have computed 9 standard status indices of all these central graphs of standard graphs.

Keywords: The (a, b) – status index, first and second status indices, first and second status Gourava indices.

I. INTRODUCTION

Graphs, here considered, are connected and simple with no self-loops and no parallel edges. Vertex set is denoted by $V(G)$, edge set is denoted by $E(G)$ for a graph G . The Central graph $C(G)$ of a graph G is the graph obtained by sub-dividing each edge of a G exactly once and joining all non-adjacent vertices of G . The length of shortest path between two vertices u and v , denoted by $d(u, v)$ is distance between them. The sum of distances of a vertex u from all other vertices of a graph is called status of the vertex u with notation $\sigma(u)$. Ramane et.al [4] introduced first and second connectivity status indices. V.R.Kulli et.al introduced [3] The (a, b) – status index, as

$$S_{a,b} = \sum_{uv \in E(G)} \{(\sigma(u))^a \cdot (\sigma(v))^b + (\sigma(u))^b (\sigma(v))^a\}$$

For notations and definitions, we refer [1],[2]. In [3], V.R.Kulli et al. have found the first status index $S_1(G)$, second status index $S_2(G)$, product connectivity status index $PS(G)$, reciprocal product connectivity status index $RPS(G)$, the general second status index $S_2^a(G)$, The F_1 status index $F_1S(G)$, the first status Gourava index $SGO_1(G)$, the second status Gourava index $SGO_2(G)$, the symmetric division status index $SDS(G)$ of wheel and friendship graphs. Here we have obtained these indices for central graphs of star graph $K_{1,n}$, denoted by $C(K_{1,n})$, cycle graph C_n , denoted by $C(C_n)$, complete graph K_n , denoted by $C(K_n)$, wheel graph W_n with $C(W_n)$, and friendship graph F_n , denoted by $C(F_n)$.

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II. MAIN RESULTSS

Theorem 2.1. For $n \geq 2$,

$$S_{a,b} (C(K_{1,n})) = 2n\{(3n)^a(4n-2)^b + (3n)^b(4n-2)^a\} + n(n-1)(3n)^{a+b}$$

Proof. By definition of central graph, and by computation, we note that $C(K_{1,n})$ has $(2n+1)$ vertices and $\frac{n^2+3n}{2}$ edges.

The edge set $E(C(K_{1,n}))$ can be divided into the following two parts.

$$E_1 = \{uv \in E(C(K_{1,n})) / d(u) = n, d(v) = n\} \text{ and}$$

$$E_2 = \{uv \in E(C(K_{1,n})) / d(u) = n, d(v) = \frac{n(n-1)}{2}\}$$

Calculating status of every vertex of the graph, we find that

$M(K_{1,n})$ has 2 status edges as listed in Table 1.

Table 1: Details of Status of vertices of $C(K_{1,n})$

$(\sigma(u), \sigma(v)) / uv \in E(C(K_{1,n}))$	Total edges
$(3n, 4n-2)$	$2n$
$(3n, 3n)$	$\frac{n(n-1)}{2}$

Using the above table and definition, we get,

$$S_{a,b} (C(K_{1,n})) = 2n\{(3n)^a(4n-2)^b + (3n)^b(4n-2)^a\} + \frac{n(n-1)}{2}\{(3n)^a(3n)^b + (3n)^b(3n)^a\} = 2n\{(3n)^a(4n-2)^b + (3n)^b(4n-2)^a\} + n(n-1)(3n)^{a+b}$$

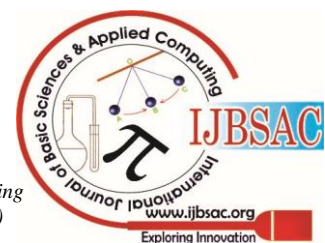
Theorem 2.2. For $n \geq 2$,

$$SGO_1 (C(K_{1,n})) = \frac{9n^4 + 45n^3 - 2n^2 - 8n}{2}$$

Proof. By definition of first Gourava index [3], we have

$$SGO_1 (C(K_{1,n})) = \sum_{uv \in E(C(K_{1,n}))} \{\sigma(u) + \sigma(v) + \sigma(u)\sigma(v)\}$$

Using table 1, we note that



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$$\begin{aligned} SGO_1(C(K_{1,n})) &= 2n\{3n + (4n - 2) + 3n(4n - 2)\} \\ &+ \frac{n(n-1)}{2}\{3n + 3n + 9n^2\} \\ &= \frac{9n^4 + 45n^3 - 2n^2 - 8n}{2} \end{aligned}$$

Corollary 2.3.

1. The first status index

$$\begin{aligned} S_1(C(K_{1,n})) &= S_{1,0}(C(K_{1,n})) \\ &= 3n^3 + 11n^2 - 4n \end{aligned}$$

2. The second status index

$$\begin{aligned} S_2(C(K_{1,n})) &= \frac{1}{2}(S_{1,1}(C(K_{1,n}))) \\ &= \frac{9n^4 + 39n^3 - 24n^2}{2} \end{aligned}$$

3. The product connectivity status index

$$\begin{aligned} PS(C(K_{1,n})) &= \frac{1}{2}\left(S_{\frac{-1}{2}, \frac{-1}{2}}(C(K_{1,n}))\right) \\ &= \frac{2n}{\sqrt{12n^2 - 6n}} + \frac{(n-1)}{6} \end{aligned}$$

4. The reciprocal product connectivity status index

$$\begin{aligned} RPS(C(K_{1,n})) &= \frac{1}{2}\left(S_{\frac{1}{2}, \frac{1}{2}}(C(K_{1,n}))\right) \\ &= 2n\sqrt{12n^2 - 6n} + \frac{3n^3 - 3n}{2} \end{aligned}$$

5. The general second status index

$$\begin{aligned} S_2^a(C(K_{1,n})) &= \frac{1}{2}(S_{a,a}(C(K_{1,n}))) \\ &= 2n(3n)^a(4n - 2)^a + \frac{n(n-1)(3n)^{2a}}{2} \end{aligned}$$

6. The F_1 status index

$$\begin{aligned} F_1S(C(K_{1,n})) &= S_{2,0}(C(K_{1,n})) \\ &= 9n^4 + 41n^3 - 32n^2 + 8n \end{aligned}$$

7. The second status Gourava Index

$$\begin{aligned} SGO_2(C(K_{1,n})) &= S_{2,1}(C(K_{1,n})) \\ &= 27n^5 + 141n^4 - 132n^3 + 24n^2 \end{aligned}$$

8. The symmetric division status index

$$\begin{aligned} SDS(C(K_{1,n})) &= S_{1,-1}(C(K_{1,n})) \\ &= 2n\left(\frac{3n}{4n-2} + \frac{4n-2}{3n}\right) + n(n-1) \end{aligned}$$

Theorem 2.4. For $n \geq 2$

$$\begin{aligned} S_{a,b}(C(C_n)) &= 2n((3n-1)^a(5n-7)^b \\ &+ (3n-1)^b(5n-7)^a \\ &+ (n^2-3n)(3n-1)^{a+b} \end{aligned}$$

Proof. By definition of central graph, and by computation, we note that $C(C_n)$ has $2n$ vertices and $\frac{n^2+n}{2}$ edges. The edge set $E(C(C_n))$ can be divided into the following two parts.

$$E_1 = \{uv \in E(C(C_n)) / d(u) = n-1, d(v) = 2\}$$

$$E_2 = \{uv \in E(C(C_n)) / d(u) = n-1, d(v) = n-1\}$$

Calculating status of each vertex of the graph, we find that $(C(C_n))$ has the following two types of status edges:

Table 2: Details of status of vertices of $C(C_n)$

$(\sigma(u), \sigma(v)) / uv \in E(C(C_n))$	Total edges
$(3n-1, 5n-7)$	$2n$
$(3n-1, 3n-1)$	$\frac{n^2-3n}{2}$

Using the above table and definition, we get,

$$\begin{aligned} S_{a,b}(C(C_n)) &= 2n((3n-1)^a(5n-7)^b \\ &+ (3n-1)^b(5n-7)^a \\ &+ \left(\frac{n^2-3n}{2}\right)((3n-1)^a(3n-1)^b \\ &+ (3n-1)^a(3n-1)^b) \end{aligned}$$

$$\begin{aligned} S_{a,b}(C(C_n)) &= 2n\left(\frac{(3n-1)^a(5n-7)^b + (3n-1)^b(5n-7)^a}{2}\right) \\ &+ (n^2-3n)(3n-1)^{a+b} \end{aligned}$$

Theorem 2.5. For $n \geq 3$,

$$SGO_1(C(C_n)) = \frac{9n^4 + 33n^3 - 73n^2 - n}{2}$$

Proof: By definition of first Gourava index[3], we have

$$SGO_1(C(C_n)) = \sum_{uv \in E(C(C_n))} \{\sigma(u) + \sigma(v) + \sigma(u)\sigma(v)\}$$

Using table 2, we note that

$$\begin{aligned} SGO_1(C(C_n)) &= 2n\left(\frac{(3n-1) + (5n-7)}{2}\right) \\ &+ \left(\frac{n^2-3n}{2}\right)\left(\frac{(3n-1) + (3n-1)}{2}\right) \\ &+ (3n-1)^2 \\ &= \frac{9n^4 + 33n^3 - 73n^2 - n}{2} \end{aligned}$$

Corollary 2.6.

$$1. S_1(C(C_n)) = S_{1,0}(C(C_n)) = 3n^3 + 6n^2 - 13n$$

$$2. S_2(C(C_n)) = \frac{1}{2}(S_{1,1}(C(C_n)))$$



$$= \frac{9n^4 + 27n^3 - 85n^2 + 25n}{2}$$

$$3. PS(C(C_n)) = \frac{1}{2} \left(S_{\frac{-1}{2}, \frac{-1}{2}}(C(C_n)) \right) \\ = \frac{2n}{\sqrt{(15n^2 - 26n + 7)}} + \frac{n^2 - 3n}{(6n - 2)}$$

$$4. RPS(C(C(C_n))) = \frac{1}{2} \left(S_{\frac{1}{2}, \frac{1}{2}}(C(C_n)) \right) \\ = \frac{4n\sqrt{(n^2 - 26n + 7)} + 3n^3 - 10n^2 + 3n}{2}$$

$$5. S_2^a(C(C_n)) = \frac{1}{2} (S_{a,a}(C(C_n))) \\ = (3n - 1)^a \left(2n(5n - 7)^a + \frac{(n^2 - 3n)(3n - 1)^a}{2} \right)$$

$$6. F_1S(C(C_n)) = S_{2,0}(C(C_n)) \\ = 9n^4 + 35n^3 - 133n^2 + 97n$$

$$7. SGO_2(C(C_n)) = S_{2,1}(C(C_n)) \\ = 27n^5 + 132n^4 - 566n^3 + 500n^2 - 109n$$

$$8. SDS(C(C_n)) = S_{1,-1}(C(C_n)) \\ = 2n \left(\frac{3n-1}{5n-7} + \frac{5n-7}{3n-1} \right) + (n^2 - 3n)$$

Theorem 2.7. For $n \geq 4$

$$S_{a,b}(C(K_n)) = n^{a+b+1} \left(\left(\frac{3n-3}{2} \right)^a (2n-3)^b + \left(\frac{3n-3}{2} \right)^b (2n-3)^a + (n-2) \right)$$

Proof. By definition of central graph, and by computation, we note that $C(K_n)$ has $\frac{n^2+n}{2}$ vertices and $n(n-1)$ edges.

$E(C(K_n))$ can be written as

$$E = \{uv \in E(C(K_n)) / d(u) = n-1, d(v) = 2\}$$

Calculating status of every vertex, we find that $(C(K_n))$ has the following status edges:

Table 3: Details of status of vertices of $C(K_n)$

$(\sigma(u), \sigma(v)) / uv \in E(C(K_n))$	Total edges
$\left(\frac{3n^2 - 3n}{2}, 2n^2 - 3n \right)$	$n(n-1)$

Using the above table and definition, we get,

$$S_{a,b}(C(K_n)) = n(n-1)$$

$$\left(\left(\frac{3n^2 - 3n}{2} \right)^a (2n^2 - 3n)^b + (2n^2 - 3n)^a \left(\frac{3n^2 - 3n}{2} \right)^b \right) \\ = n^{a+b+1}(n-1)$$

$$\left(\left(\frac{3n-3}{2} \right)^a (2n-3)^b + \left(\frac{3n-3}{2} \right)^b (2n-3)^a \right)$$

Theorem 2.8. For $n \geq 2$

$$SGO_1(C(K_n)) = \frac{6n^6 - 21n^5 + 31n^4 - 25n^3 + 9n^2}{2}$$

Proof. By definition of first Gourava index[3], we have

$$SGO_1(C(K_n)) = \sum_{uv \in E(C(K_n))} \{\sigma(u) + \sigma(v) + \sigma(u)\sigma(v)\}$$

Using table 3, we note that

$$SGO_1(C(K_n)) = n(n-1) \left(\left(\frac{3n^2 - 3n}{2} \right) + (2n^2 - 3n) + \left(\frac{3n^2 - 3n}{2} \right) (2n^2 - 3n) \right) \\ = \frac{6n^6 - 21n^5 + 31n^4 - 25n^3 + 9n^2}{2}$$

Corollary 2.9.

$$1. S_1(C(K_n)) = S_{1,0}(C(K_n)) = \frac{7n^4 - 162n^3 + 9n^2}{2}$$

$$2. S_2(C(K_n)) = \frac{1}{2} (S_{1,1}(C(K_n))) = \frac{3n^3(n-1)^2(2n-3)}{2}$$

$$3. PS(C(K_n)) = \frac{1}{2} \left(S_{\frac{-1}{2}, \frac{-1}{2}}(C(K_n)) \right) \\ = \frac{\sqrt{2}(n-1)}{\sqrt{6n^2 - 15n + 9}}$$

$$4. RPS(C(K_n)) = \frac{1}{2} \left(S_{\frac{1}{2}, \frac{1}{2}}(C(K_n)) \right) \\ = \frac{\sqrt{3}}{\sqrt{2}} \left(n^2(n-1)\sqrt{2n^2 - 5n + 3} \right)$$

$$5. S_2^a(C(K_n)) = \frac{1}{2} (S_{a,a}(C(K_n))) \\ = \frac{n^{2a+1}(n-1)(3n-3)^a(2n-3)^a}{2}$$

$$6. F_1S(C(K_n)) = S_{2,0}(C(K_n)) \\ = \frac{25n^6 - 91n^5 + 111n^4 - 45n^3}{4}$$

$$7. SGO_2(C(K_n)) = S_{2,1}(C(K_n)) \\ = \frac{42n^8 - 201n^7 + 357n^6 - 279n^5 + 81n^4}{4}$$

$$8. SDS(C(K_n)) = S_{1,-1}(C(K_n))$$



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$$= n(n-1) \left(\frac{3n-3}{2(2n-3)} + \frac{2(2n-3)}{3n-3} \right)$$

Theorem 2.10.

$$\begin{aligned} S_{a,b}(C(W_n)) &= 2n((5n+2)^a(8n-6)^b \\ &\quad + (5n+2)^b(8n-6)^a) \\ &\quad + n((5n+2)^a(7n-2)^b \\ &\quad + (5n+2)^b(7n-2)^a) \\ &\quad + n((7n-2)^a(6n)^b + (7n-2)^b(6n)^a) \\ &\quad + (n^2-3n)(5n+2)^{a+b} \end{aligned}$$

Proof. By definition of central graph, and by computation, we note that $C(W_k)$ with $k = n + 1$ has $3n + 1$ vertices and $\left(\frac{n^2+5n}{2}\right)$ edges. The edge set $E(C(W_k))$ can be divided into the following two parts.

$$E_1 = \{uv \in E(C(W_k)) / d(u) = n, d(v) = 2\}$$

$$E_2 = \{uv \in E(C(W_k)) / d(u) = n, d(v) = n\}$$

Calculating status of every vertex, we find that $(C(W_k))$ has the following four types of status edges:

Table 4: Details of status of vertices of $C(W_n)$

$(\sigma(u), \sigma(v)) / uv \in E(C(W_n))$	Total edges
$(5n + 2, 8n - 6)$	$2n$
$(5n + 2, 7n - 2)$	n
$(7n - 2, 6n)$	n
$(5n + 2, 5n + 2)$	$\frac{n^2 - 3n}{2}$

Using the above table and definition, we get,

$$\begin{aligned} S_{a,b}(C(W_n)) &= 2n((5n+2)^a(8n-6)^b \\ &\quad + (5n+2)^b(8n-6)^a) \\ &\quad + n((5n+2)^a(7n-2)^b \\ &\quad + (5n+2)^b(7n-2)^a) \\ &\quad + n((7n-2)^a(6n)^b + (7n-2)^b(6n)^a) \\ &\quad + (n^2-3n)(5n+2)^{a+b} \end{aligned}$$

Theorem 2.11. For $n \geq 3$

$$SGO_1(C(W_n)) = \frac{25n^4 + 269n^3 - 52n^2 - 100n}{2}$$

Proof. By definition of first Gourava index[3], we have

$$SGO_1(C(W_n)) = \sum_{uv \in E(C(W_k))} \{\sigma(u) + \sigma(v) + \sigma(u)\sigma(v)\}$$

Using table 4, we note that

$$\begin{aligned} SGO_1(C(W_n)) &= 2n((5n+2) + (8n-6) \\ &\quad + (5n+2)(8n-6)) \end{aligned}$$

$$\begin{aligned} &+ n((5n+2) + (7n-2) \\ &\quad + (5n+2)(7n-2)) \\ &\quad + n((7n-2) + 6n + 6n(7n-2)) \\ &\quad + \left(\frac{n^2-3n}{2}\right)((5n+2) + (5n+2) \\ &\quad + (5n+2)^2) \\ &= \frac{25n^4 + 269n^3 - 52n^2 - 100n}{2} \end{aligned}$$

Corollary 2.12.

$$\begin{aligned} 1. S_1(C(W_n)) &= S_{1,0}(C(W_k)) \\ &= 5n^3 + 38n^2 - 16n \end{aligned}$$

$$\begin{aligned} 2. S_2(C(W_n)) &= \frac{1}{2}(S_{1,1}(C(W_k))) \\ &= \frac{25n^4 + 259n^3 - 128n^2 - 68n}{2} \end{aligned}$$

$$\begin{aligned} 3. PS(C(W_n)) &= \frac{1}{2}(S_{\frac{-1}{2}, \frac{-1}{2}}(C(W_k))) \\ &= \frac{2n}{\sqrt{40n^2 - 14n - 12}} + \frac{n}{\sqrt{35n^2 + 14n - 4}} \\ &\quad + \frac{n}{\sqrt{42n^2 - 12n}} + \frac{n^2 - 3n}{(10n + 4)} \end{aligned}$$

$$\begin{aligned} 4. RPS(C(W_n)) &= \frac{1}{2}(S_{\frac{1}{2}, \frac{1}{2}}(C(W_k))) \\ &= 2n\sqrt{40n^2 - 14n - 12} \\ &\quad + n\sqrt{35n^2 + 14n - 4} \\ &\quad + n\sqrt{42n^2 - 12n} + \frac{(n^2 - 3n)(5n + 2)}{2} \end{aligned}$$

$$\begin{aligned} 5. S_2^a(C(W_n)) &= \frac{1}{2}(S_{a,a}(C(W_k))) \\ &= 2n(5n+2)^a(8n-6)^a \\ &\quad + n(5n+2)^a(7n-2)^a \\ &\quad + n(7n-2)^a(6n)^a \\ &\quad + \frac{(n^2-3n)(5n+2)^{2a}}{2} \end{aligned}$$

$$\begin{aligned} 6. F_1S(C(W_n)) &= S_{2,0}(C(W_n)) \\ &= 25n^4 + 282n^3 - 244n^2 + 80n \end{aligned}$$

$$\begin{aligned} 7. SGO_2(C(W_n)) &= S_{2,1}(C(W_k)) \\ &= 125n^5 + 1781n^4 - 1266n^3 - 396n^2 \\ &\quad + 72n \end{aligned}$$

$$8. SDS(C(W_n)) = S_{1,-1}(C(W_n))$$



$$= 2n \left(\frac{5n+2}{8n-6} + \frac{8n-6}{5n+2} \right) + n \left(\frac{5n+2}{7n-2} + \frac{7n-2}{5n+2} \right) + n \left(\frac{7n-2}{6n} + \frac{6n}{7n-2} \right) + (n^2 - 3n)$$

Theorem 2.13.

$$S_{a,b}(C(F_n)) = 2n(8n+1)^a(13n-4)^b + (8n+1)^b(13n-4)^a + 2n(8n+1)^a(11n-2)^b + (8n+1)^b(11n-2)^a + 2n((11n-2)^a(9n)^b + 11n-2)^b(9n)^a + 2(2n^2-2n)(8n+1)^{a+b}$$

Proof. By definition of central graph, and by computation, we note that $C(F_n)$ has $(5n+1)$ vertices and $(2n^2+4n)$ edges. The edge set $E(C(F_n))$ can be divided into the following two parts.

$$E_1 = \{uv \in E(M(F_n)) / d(u) = 2n, d(v) = 2\} \text{ and } E_2 = \{uv \in E(M(F_n)) / d(u) = 2n, d(v) = 2n\}$$

Calculating status of every vertex, we find that $(C(F_n))$ has the following four types of status edges:

Table 5: Details of status of vertices of $C(F_n)$

$(\sigma(u), \sigma(v)) / uv \in E(C(F_n))$	Total edges
$(8n+1, 13n-4)$	$2n$
$(8n+1, 11n-2)$	$2n$
$(11n-2, 9n)$	$2n$
$(8n+1, 8n+1)$	$2n^2-2n$

Using the above table and definition, we get,

$$S_{a,b}(C(F_n)) = 2n(8n+1)^a(13n-4)^b + (8n+1)^b(13n-4)^a + 2n(8n+1)^a(11n-2)^b + (8n+1)^b(11n-2)^a + 2n((11n-2)^a(9n)^b + 11n-2)^b(9n)^a + 2(2n^2-2n)(8n+1)^{a+b}$$

Theorem 2.14. For $n \geq 2$

$$SGO_1(C(F_n)) = 128n^4 + 518n^3 - 22n^2 - 30n$$

Proof. By definition of first Gourava index, we have

$$SGO_1(C(F_n)) = \sum_{uv \in E(C(F_n))} \{\sigma(u) + \sigma(v) + \sigma(u)\sigma(v)\}$$

Using table 5, we note that

$$SGO_1(C(F_n)) = 2n((8n+1) + (13n-4) + (8n+1)(13n-4) + 2n((8n+1) + (11n-2) + (8n+1)(11n-2) + 2n((11n-2) + (9n) + 9n(11n-2) + (2n^2-2n)((8n+1) + (8n+1) + (8n+1)(8n+1)) = 128n^4 + 518n^3 - 22n^2 - 30n$$

Corollary 2.15.

- $S_1(C(F_n)) = S_{1,0}(C(F_n)) = 32n^3 + 92n^2 - 16n$
- $S_2(C(F_n)) = \frac{1}{2}(S_{1,1}(C(F_n))) = 128n^4 + 486n^3 - 114n^2 - 14n$
- $PS(C(F_n)) = \frac{1}{2} \left(S_{\frac{-1}{2}, \frac{-1}{2}}(C(F_n)) \right) = \frac{2n}{\sqrt{104n^2-19n-4}} + \frac{2n}{\sqrt{88n^2-5n-2}} + \frac{2n}{\sqrt{99n^2-18n}} + \frac{4n^2-4n}{(8n+1)}$
- $RPS(C(F_n)) = \frac{1}{2} \left(S_{\frac{1}{2}, \frac{1}{2}}(C(F_n)) \right) = 2n\sqrt{104n^2-19n-4} + 2n\sqrt{88n^2-5n-2} + 2n\sqrt{99n^2-18n} + (4n^2-4n)(8n+1)$
- $S_2^a(C(F_n)) = \frac{1}{2}(S_{a,a}(C(F_n))) = 2n(8n+1)^a(13n-4)^a + 2n(8n+1)^a(11n-2)^a + 2n(11n-2)^a(9n)^a + (2n^2-2n)(8n+1)^{2a}$
- $F_1S(C(F_n)) = S_{2,0}(C(F_n)) = 256n^4 + 1048n^3 - 380n^2 + 48n$
- $SGO_2(C(F_n)) = S_{2,1}(C(F_n)) = 2048n^5 + 10392n^4 - 3567n^3 - 140n^2 + 24$
- $SDS(C(F_n)) = S_{1,-1}(C(F_n)) = 2n \left(\frac{8n+1}{13n-4} + \frac{13n-4}{8n+1} \right)$



III. CONCLUSION

In this article, we have obtained the (a, b) –status indices of central graphs of some standard graphs. We can find these indices for other derived graphs also. We can use status to define a new polynomial also.

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